

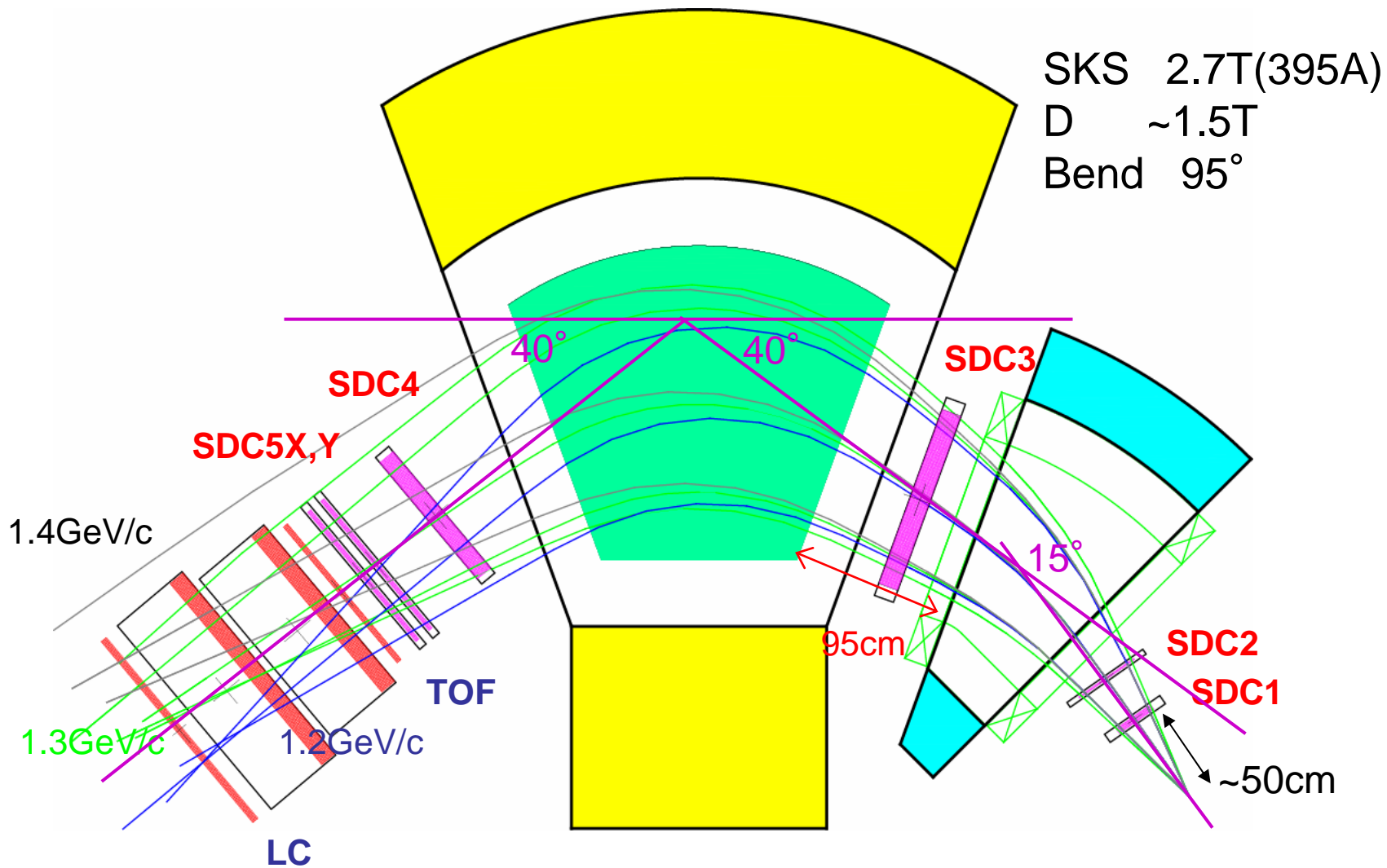
$\Xi$  hypernuclear spectroscopy  
via  $(K^-, K^+)$  reaction at J-PARC

# Overview of Proposal

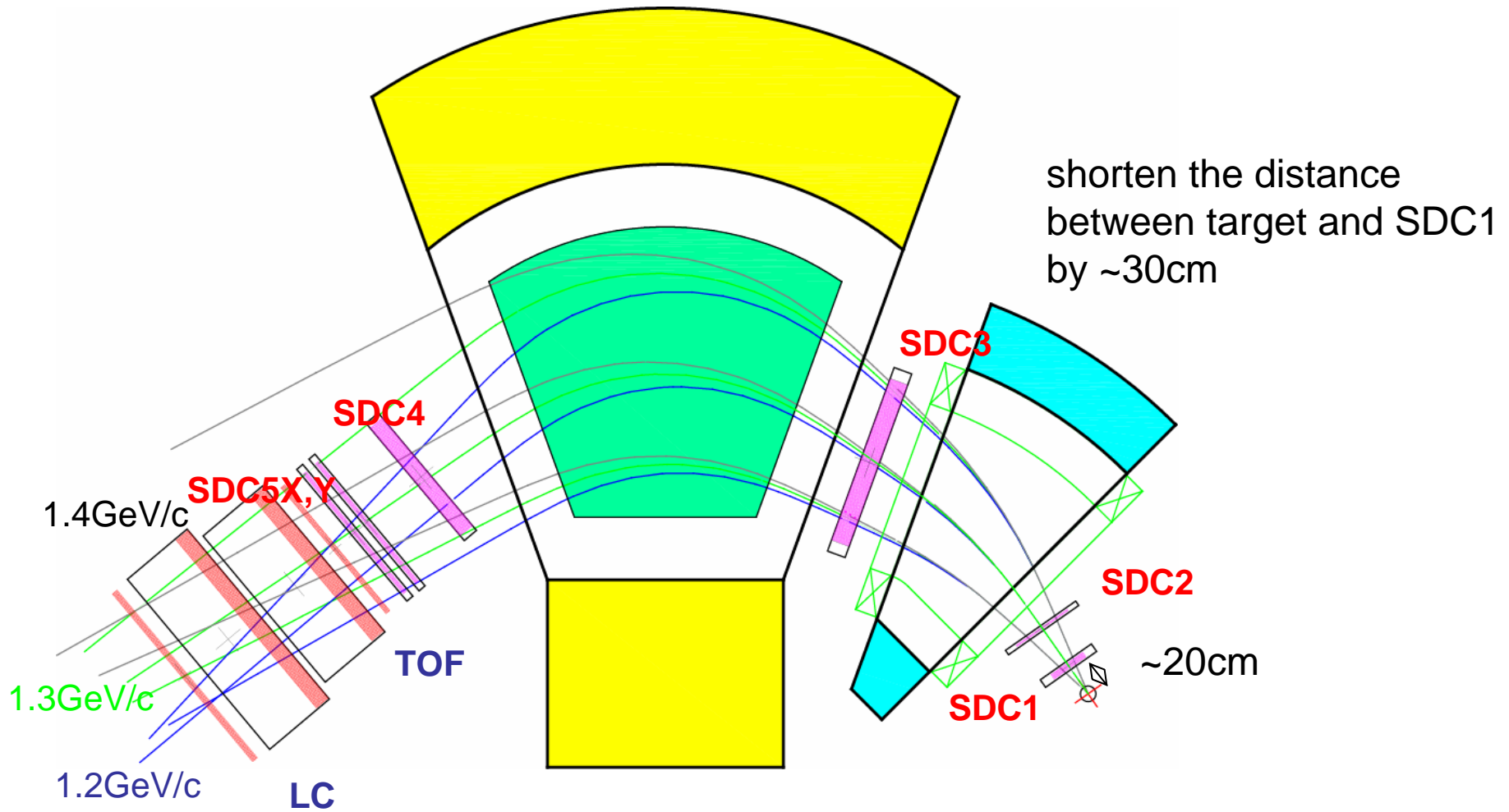
- Construction of SksPlus Spectrometer at K1.8 beamline.
- Spectrometer tuning using  $H(K^-, K^+)E^-$  reaction.
- Measurement of  $^{12}C(K^-, K^+)^{12}_E Be$  reaction.
- Measurement of  $^3He(K^-, K^+)$  reaction in future.

# SksPlus Spectrometer

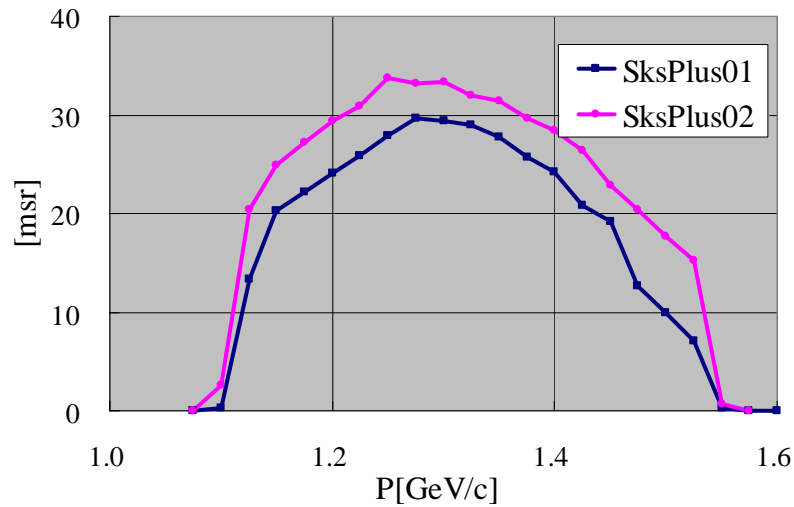
## SksPlus01



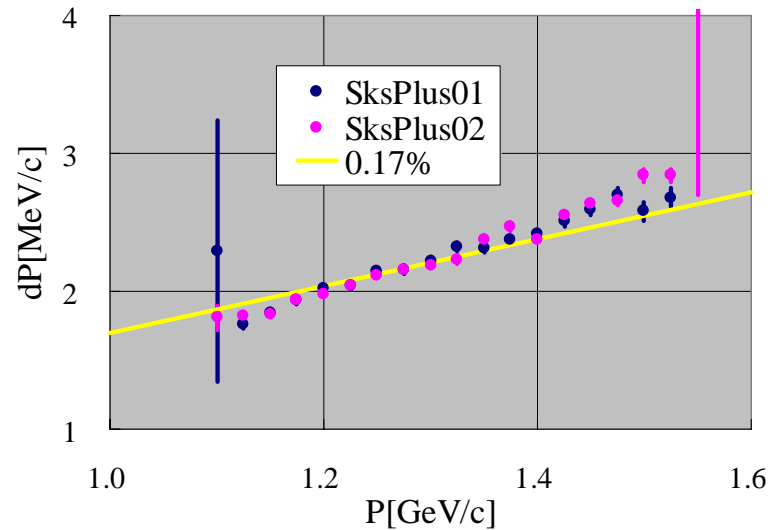
# SksPlus02



# Acceptance & Resolution by Simulation



$\Omega \sim 30 \text{msr}$  for SksPlus02



$\Delta p/p \sim 0.17\%$  (FWHM)

# Detector Size

	Size [mm <sup>2</sup> ]	configuration	rate?
SDC1	250 <sup>H</sup> x 200 <sup>V</sup>	u-u'-v-v'	Y
SDC2	400 <sup>H</sup> x 250 <sup>V</sup>	x-x'(-u-u'-v-v')	Y
SDC3	1100 <sup>H</sup> x 450 <sup>V</sup>	(3-4)x	
SDC4	900 <sup>H</sup> x 900 <sup>V</sup>	x-x'-y-y'	
SDC5XY	1000 <sup>H</sup> x 1000 <sup>H</sup>	x,y	
TOF	1050 <sup>H</sup> x 1000 <sup>H</sup>	15seg.	
LC	1400 <sup>H</sup> x 1000 <sup>H</sup>	14seg.	

# Cherenkov Detectors

$\beta^{-1}$  for particles

p [GeV/c]	$\pi$	K	p
1.2	1.007	1.083	1.270
1.3	1.006	1.071	1.234
1.4	1.005	1.062	1.204

$\pi/K$  discrimination  
Aerogel (n=1.05)

K/p discrimination

Lucite (n=1.5)

Water (n=1.33)

TOF-AC1-AC2-LC-WC

TOF1-AC1-AC2-TOF2-WC

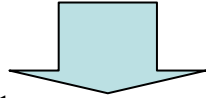
# Missing Mass Resolution

$$M^2 = (E_B + m_T - E_S)^2 - (\vec{p}_B - \vec{p}_S)^2$$

$$= m_B^2 + m_S^2 + m_T^2 + 2(m_T E_B - m_T E_S - E_B E_S + p_B p_S \cos \theta)$$

$$M \Delta M = (m_T - E_S) \Delta E_B + p_S \cos \theta \cdot \Delta p_B - (m_T + E_B) \Delta E_S$$

$$+ p_B \cos \theta \cdot \Delta p_S - p_B p_S \sin \theta \cdot \Delta \theta$$



$$\frac{\partial M}{\partial p_B} = \frac{1}{M} [\beta_B (m_T - E_S) + p_S \cos \theta],$$

$$\frac{\partial M}{\partial p_S} = -\frac{1}{M} [\beta_S (m_T + E_B) - p_B \cos \theta],$$

$$\frac{\partial M}{\partial \theta} = -\frac{p_B \cdot p_S}{M} \sin \theta$$

$$\Delta M^2 = \left( \frac{\partial M}{\partial p_B} \right)^2 \Delta p_B^2 + \left( \frac{\partial M}{\partial p_S} \right)^2 \Delta p_S^2 + \left( \frac{\partial M}{\partial \theta} \right)^2 \Delta \theta^2 + \Delta E_{\text{strag.}}^2$$



# Missing Mass Resolution

$$\Delta M^2 = \left( \frac{\partial M}{\partial p_B} \right)^2 \Delta p_B^2 + \left( \frac{\partial M}{\partial p_S} \right)^2 \Delta p_S^2 + \left( \frac{\partial M}{\partial \theta} \right)^2 \Delta \theta^2 + \Delta E_{\text{strag.}}^2$$

$\theta \sim 5^\circ$

$\text{H}(\text{K}^-, \text{K}^+) \Xi^-$

$p_B = 1.8 \text{ GeV}/c$

$p_S = 1.29 \text{ GeV}/c$

$^{12}\text{C}(\text{K}^-, \text{K}^+) ^{12}_{\Xi}\text{Be}$

$p_B = 1.8 \text{ GeV}/c$

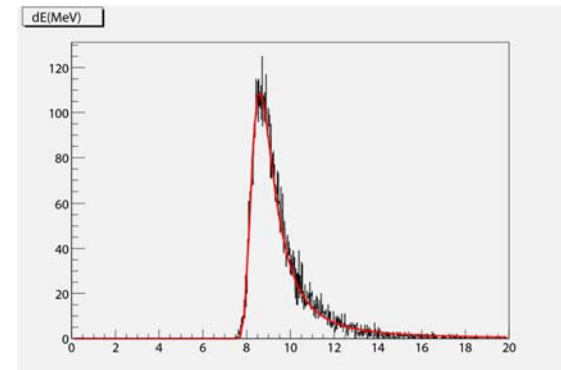
$p_S = 1.37 \text{ GeV}/c$

K1.8BS  $\Delta p/p \sim 1.4 \times 10^{-4}$  (RMS)  
 $\Delta p = 0.6 \text{ MeV}/c$  (FWHM)  
 SksPlus  $\Delta p \sim 2.5 \text{ MeV}/c$  (FWHM)  
 $\Delta \theta = 2 \text{ mrad}$

	$\Delta p_B$	$\Delta p_S$	$\Delta \theta$		$\Delta E_{\text{strag.}}$	$\Delta M$
$\text{H}(\text{K}^-, \text{K}^+) \Xi^-$	0.39	1.56	0.30	1.64		
$^{12}\text{C}(\text{K}^-, \text{K}^+) ^{12}_{\Xi}\text{Be}$	0.56	2.26	0.04	2.33	<2.0	<3.07

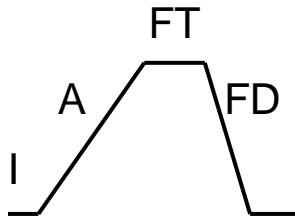
5.4g/cm<sup>2</sup> Carbon for 1.8GeV/c K<sup>-</sup>  
 MPV = 8.66MeV,  $\sigma = 0.33 \text{ MeV}$

$\Delta E_{\text{strag.}} \sim 1 \text{ MeV}$  ?



# Spill Length & Beam Intensity

PS Op. Cycle@30GeV

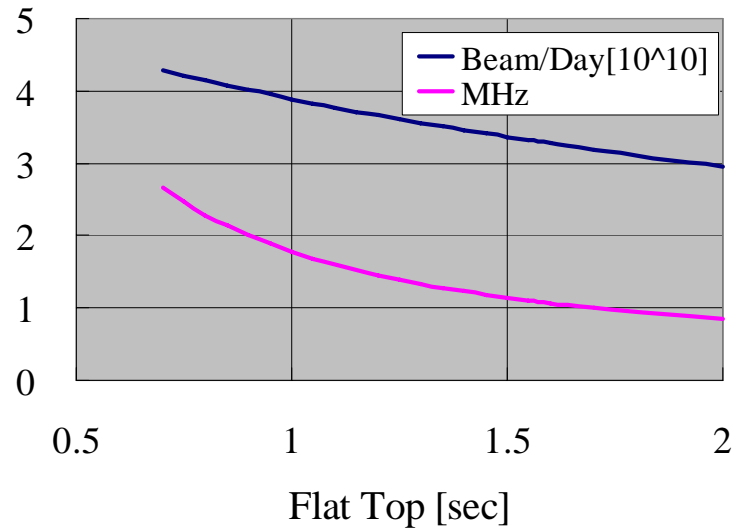


Injection	0.17s
Accelerataion	1.39s
Flat-top	0.7s –
Fall down	0.64s
Duration	2.90s –

**K<sup>-</sup> intensity at K1.8FF**  
**1.6 x 10<sup>6</sup> /spill**  
**(30GeV-9μA)**

assumed:

BeamOn time=Flat top -0.1s  
 90% efficiency



**FT 0.7-1.2sec**

**3.5x10<sup>10</sup> K<sup>-</sup>/day**



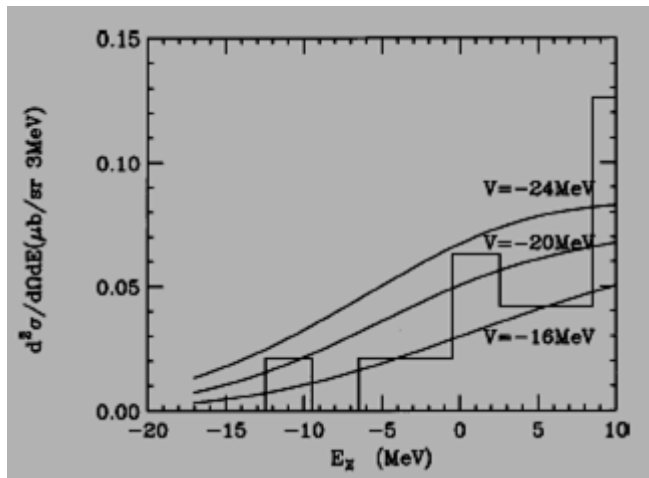
**1.5-2.5 MHz@FF**

# Previous Data on $^{12}\text{C}$

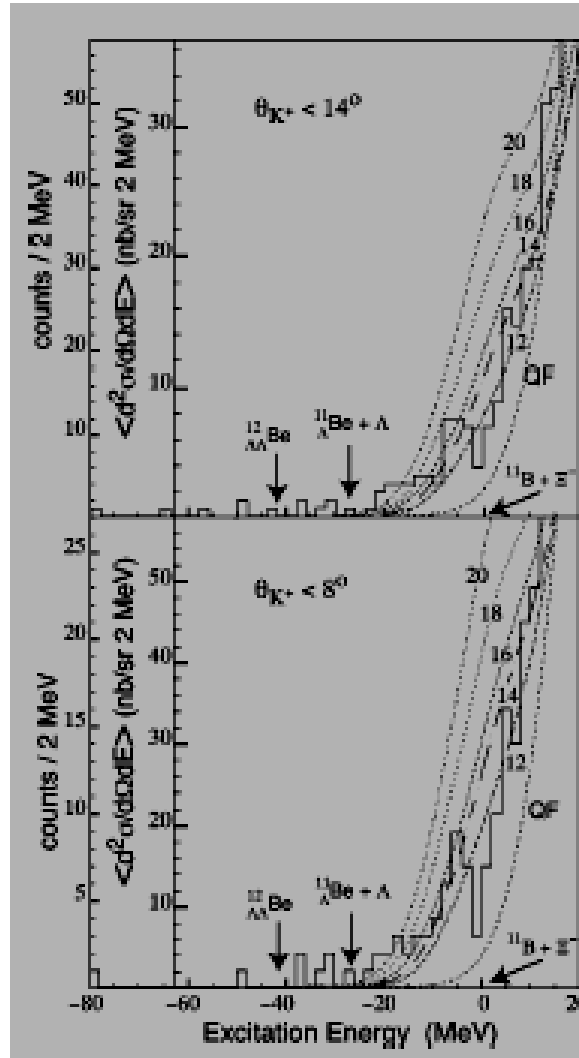
## KEK-E224

T.Fukuda et al,  
PRC58(1998)1306

$P(K^-) = 1.65\text{GeV}/c$



$0.21 \pm 0.07 \mu\text{b}/\text{sr}$   $E < 7 \text{ MeV}$   
 $60 \pm 45 \text{ nb}/\text{sr}$   $-20 < E < 0 \text{ MeV}$

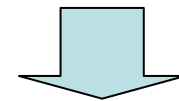


## AGS-E886

P.Khaustov et al,  
PRC61(2000)054603

$P(K^-) = 1.8\text{GeV}/c$

$-20 < E < 0 \text{ MeV}$   
 $89 \pm 14 \text{ nb}/\text{sr}$   $\theta < 8^\circ$   
 $42 \pm 5 \text{ nb}/\text{sr}$   $\theta < 14^\circ$

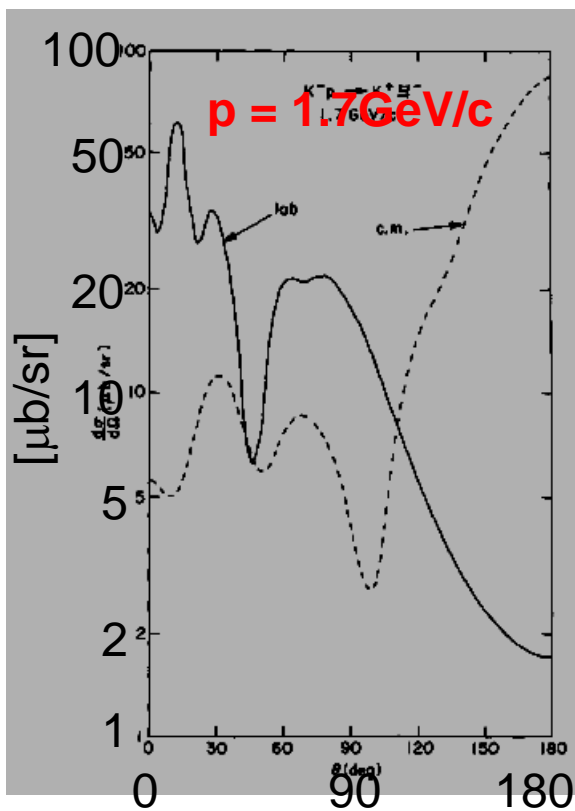


$V_{\text{eff}} = -14 \text{ MeV}$   
 Only **s-state** is bound.

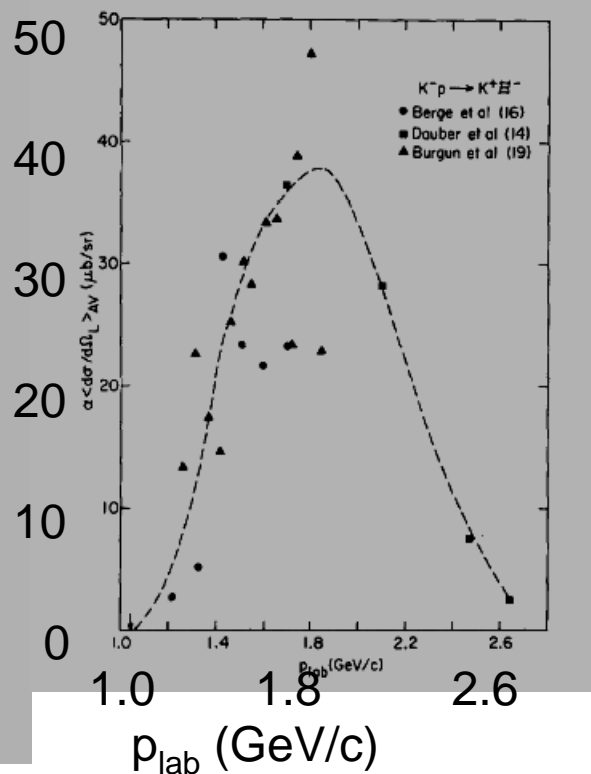
DWIA by Itonaga  
 $92 \text{ nb}/\text{sr}$   $\theta < 8^\circ$   
 $37 \text{ nb}/\text{sr}$   $\theta < 14^\circ$

# $p + K^- \rightarrow K^+ + \Xi^-$ Reaction

C.B.Dover & A.Gal  
Ann. of Phys. 146(1983)309



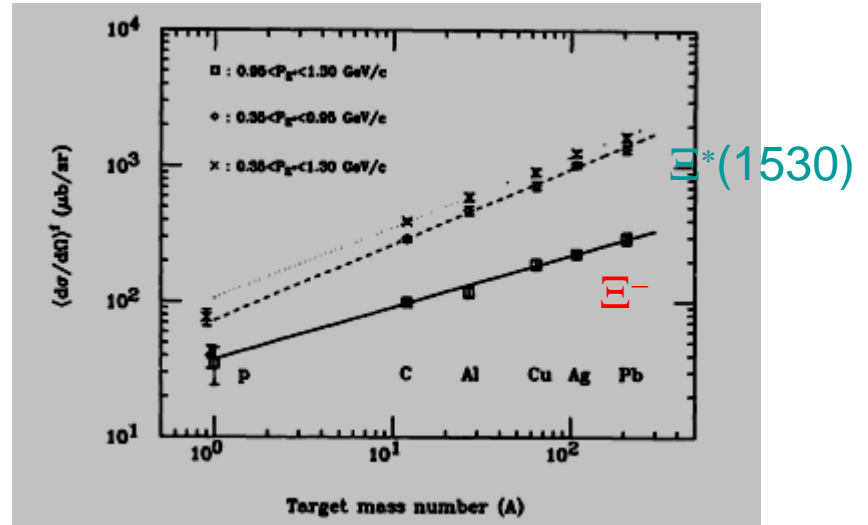
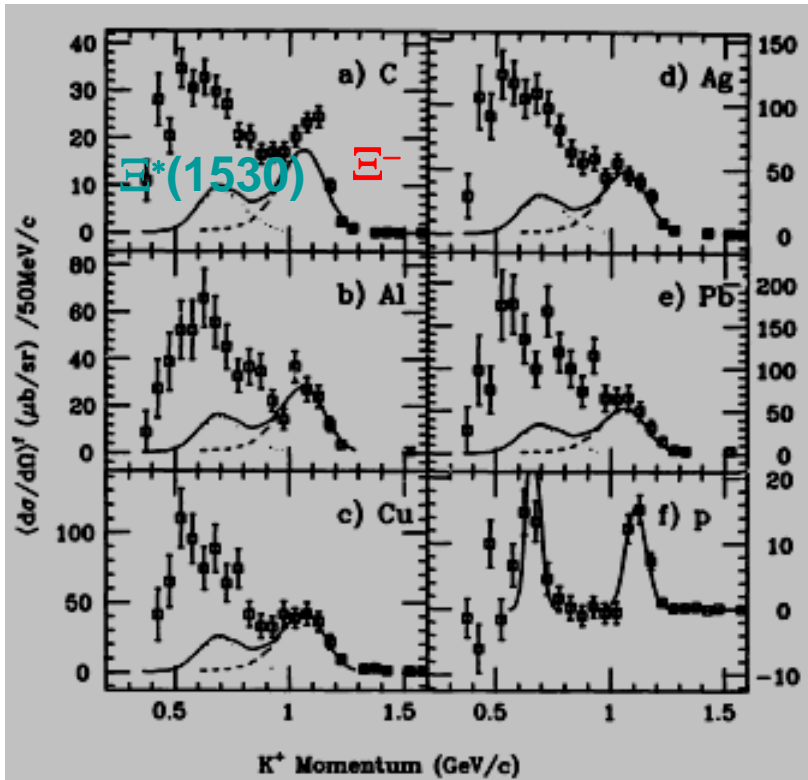
T.Iijima et al.  
NPA546(1992)588



$p = 1.65 \text{ GeV/c}$   
 $1.7^\circ < \theta_{\text{lab}} < 13.6^\circ$   
 $35 \pm 4 \mu\text{b/sr}$

# $p + K^- \rightarrow K^+ + \Xi^-$ (Quasi-Free)

T. Iijima et al.  
NPA546(1992)588



for  $\Xi^-$  production  
 $d\sigma/d\Omega = CA^\alpha$   
 $C = 37 \pm 4 \mu\text{b/sr}$   
 $\alpha = 0.56 \pm 0.02$

# Yield Estimation for $^{12}\text{C}(\text{K}^-, \text{K}^+)^{12}_{\text{E}}\text{Be}$

5.4 g/cm<sup>2</sup> (3cm) target

$$\begin{aligned} N_{\text{tgt}} &= 5.4 \times 6.02 \times 10^{-7} [\mu\text{b}^{-1}] / 12 \\ &= 2.7 \times 10^{-7} [\mu\text{b}^{-1}] \end{aligned}$$

$$N_{\text{beam}} = 3.5 \times 10^{10} [\text{/day}]$$

$$\Omega = 0.030$$

$$\text{Surv. Rate} = 0.5$$

$$\text{Ana. Efficiency} = 0.5$$

$$d\sigma/d\Omega = 0.04 [\mu\text{b}/\text{sr}]$$

$$\begin{aligned} N &= 2.7 \times 10^{-7} \times 3.5 \times 10^{10} \times 0.04 \times 0.030 \times 0.5 \times 0.5 \\ &= 2.83 [\text{/day}] \\ &\sim 20 [\text{/week}] \\ &\sim 85 [\text{/month}] \end{aligned}$$

2 months beam time is required at Phase1 beam intensity.

# Yield for $H(K^-, K^+)E^-$

CH<sub>2</sub> target (5 g/cm<sup>2</sup>)

$$N_H = 5 \times 6.02 \times 10^{-23} \times (2/14) \\ = 4.3 \times 10^{-22} [\mu\text{b}^{-1}]$$

$$N_C = 2.15 \times 10^{-22} [\mu\text{b}^{-1}]$$

Liq.-H<sub>2</sub> target (10cm)

$$\rho = 0.07 \text{ g/cm}^3$$

$$N_H = 0.07 \times 10 \times 6.02 \times 10^{-23} / 1 \\ = 4.2 \times 10^{-22} [\mu\text{b}^{-1}]$$

$$N = 4.3 \times 10^{-22} \times 3.5 \times 10^{10} \times 35 \times 0.030 \times 0.5 \times 0.5 \\ = 3.95 \times 10^3 \text{ [/day]}$$

Enough Statistics for Spectrometer Calibration

# $^3\text{He}$ Target

From Ishimoto-San's Information

- Boiling Point 3.19 K [ 4.215K ]
- density@B.P. 0.0589 g/cm<sup>3</sup> [ 0.125g/cm<sup>3</sup> ]
- Liquid quantity ~1000cm<sup>3</sup>

if 6cm $\phi$  cylinder cell , L=35cm

L=20cm

$$N_T = 0.0589 \times 20 \times 6.02 \times 10^{-7} / 3 \\ = 2.36 \times 10^{-7} [\mu\text{b}^{-1}]$$

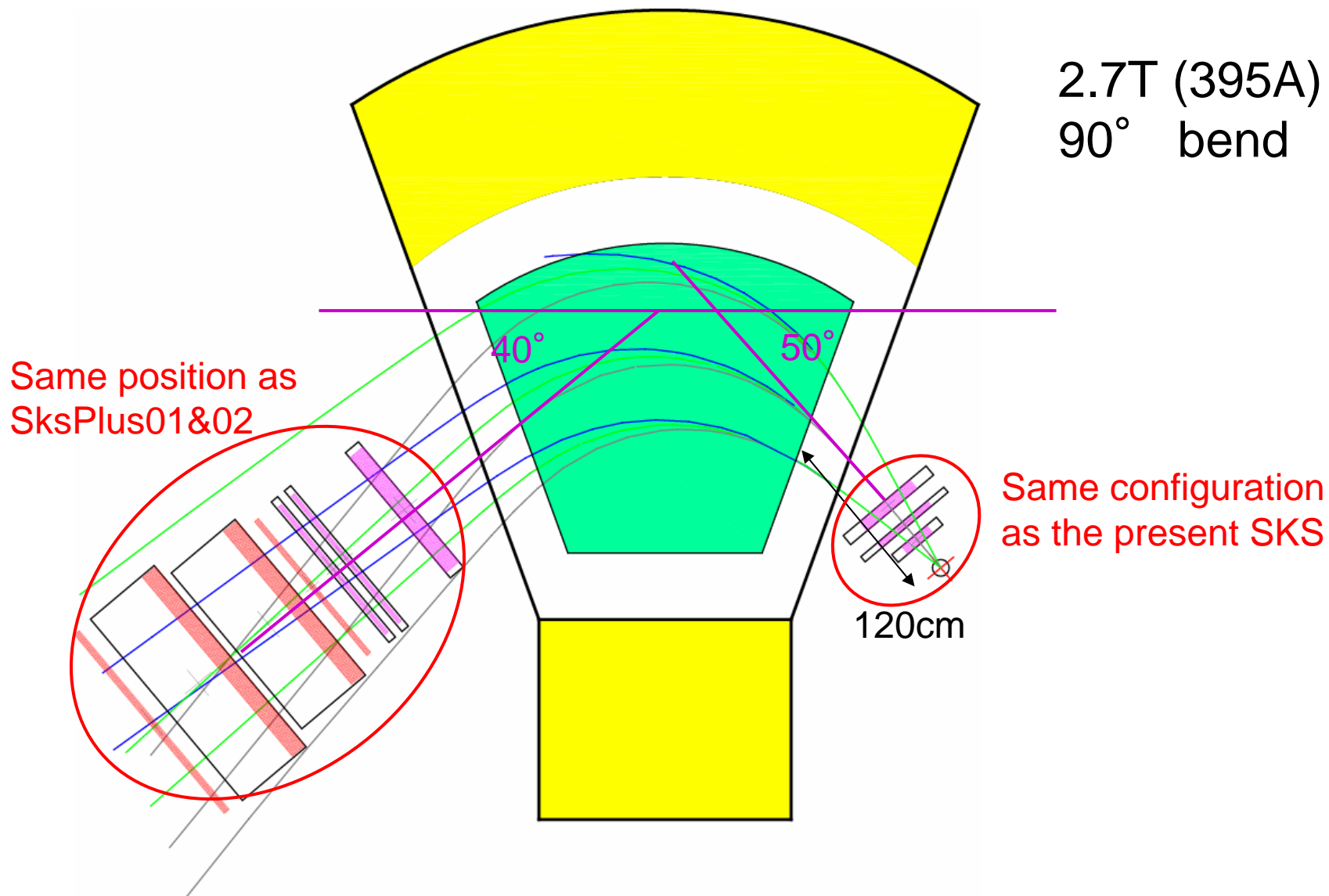
Target density is same as C case.

Cross Section ?

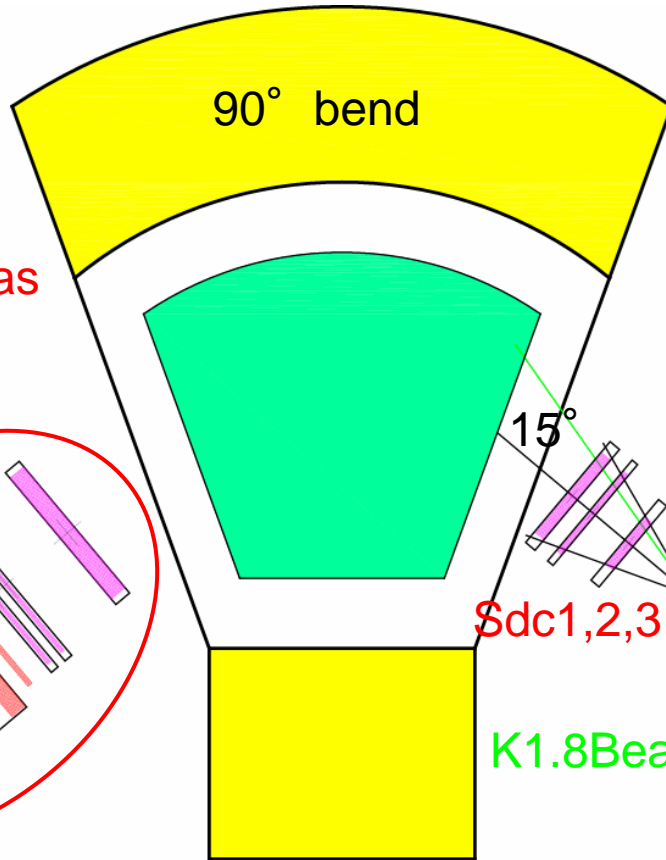
Does bound state exist ?



# Sks Single Spectrometer SksMinus02



# SksMinus04



Sks position is same as SksPlus02.  
The dipole is removed.  
New sdc1-3 are installed.

HyperBall Experiment  
with  $(K^-, \pi^-)$  at 1.5 GeV/c

FF for SksMinus04 configuration

126cm

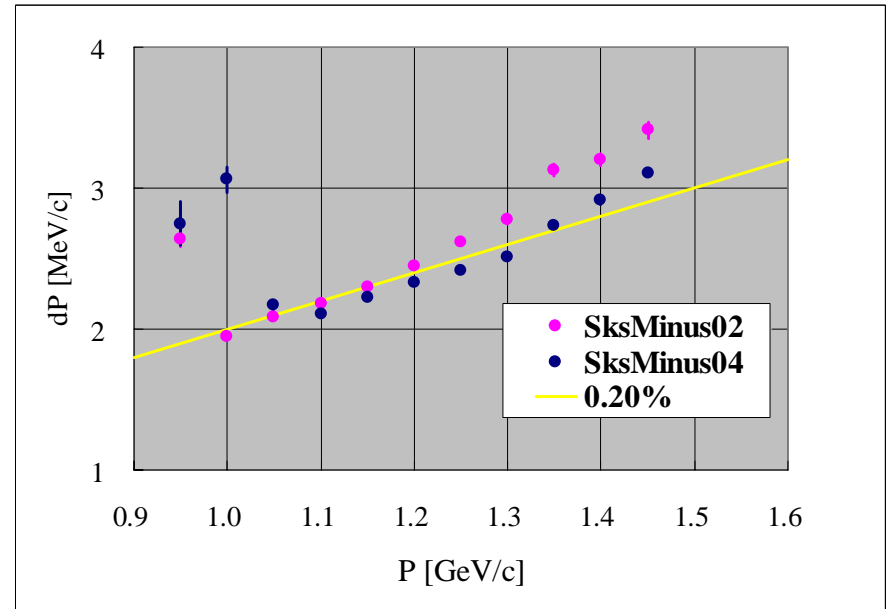
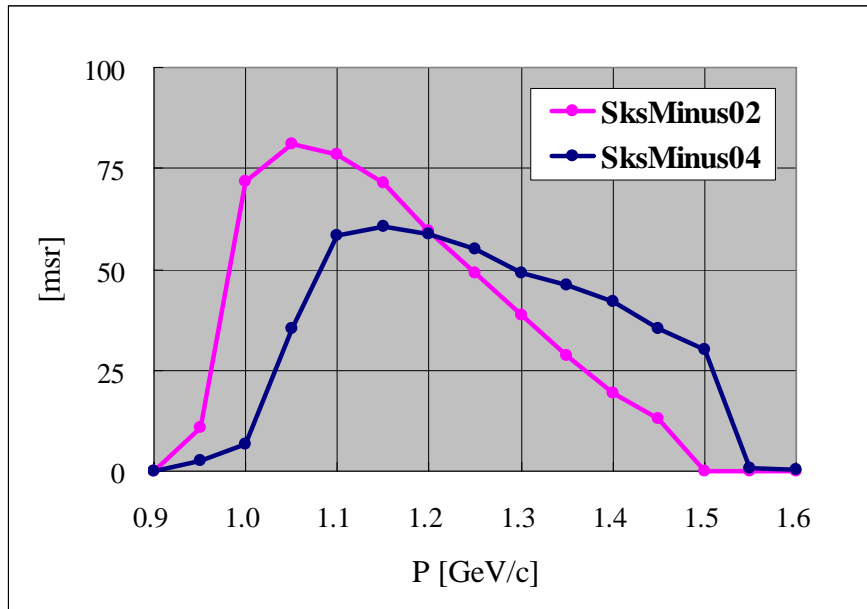
K1.8 Beamline

FF for SksPlus02 configuration

2.7T (395A)

Same position as  
SksPlus01&02

# Acceptance & Resolution for Sks Single Spectrometers



# Comparison between SksPlus02 and SksMinus02

		SksPlus02	SksMinus02
p(K <sup>-</sup> )	[GeV/c]	1.8	1.65
p(K <sup>+</sup> )	[GeV/c]	1.15–1.45	1.0–1.3
Intensity	[/spill]	1.6x10 <sup>6</sup>	0.8x10 <sup>6</sup> *
Solid Angle	[msr]	30	60
Flight Path	[m]	~7	~5
Survival Rate		~0.50	~0.57
$\Delta M(\text{FWHM})^{**}$	[MeV/c <sup>2</sup> ]		
<sup>12</sup> C(K <sup>-</sup> ,K <sup>+</sup> ) <sup>12</sup> <sub>Ξ</sub> Be		2.33	3.16
p(K <sup>-</sup> ,K <sup>+</sup> ) <sub>Ξ<sup>-</sup></sub>		1.64	2.14

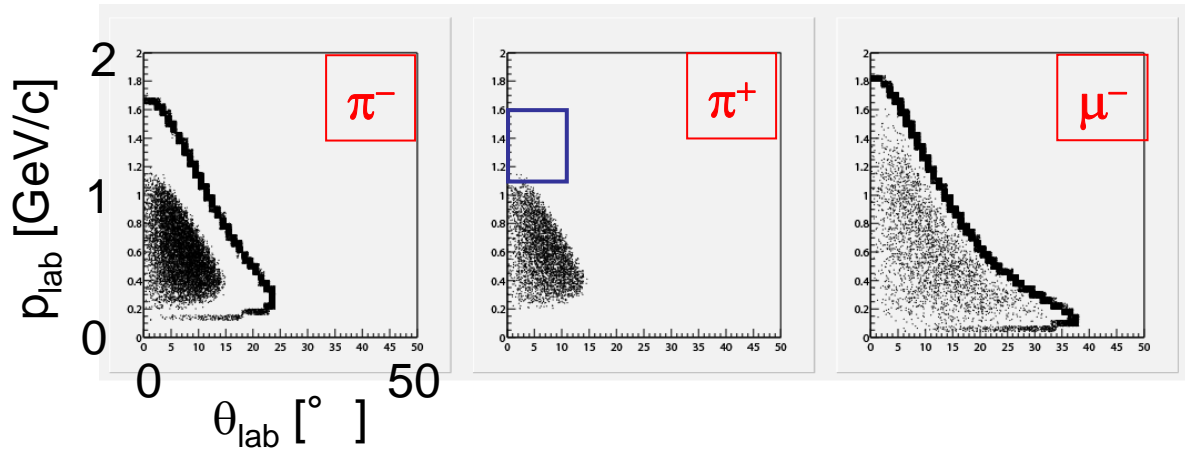
\* Naive estimation by Noumi  
 \*\* without energy loss straggling at the target.

If cross section is same at both incident momenta.

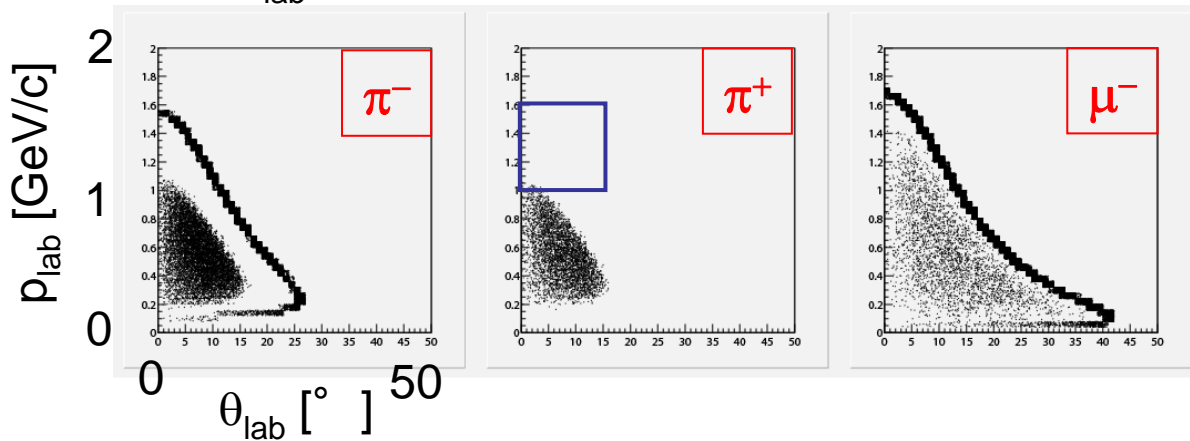
Yield gain is only 10% thanks to the short flight path.  
 Energy resolution becomes worse.

# Backgrounds –decays–

K<sup>-</sup> decays



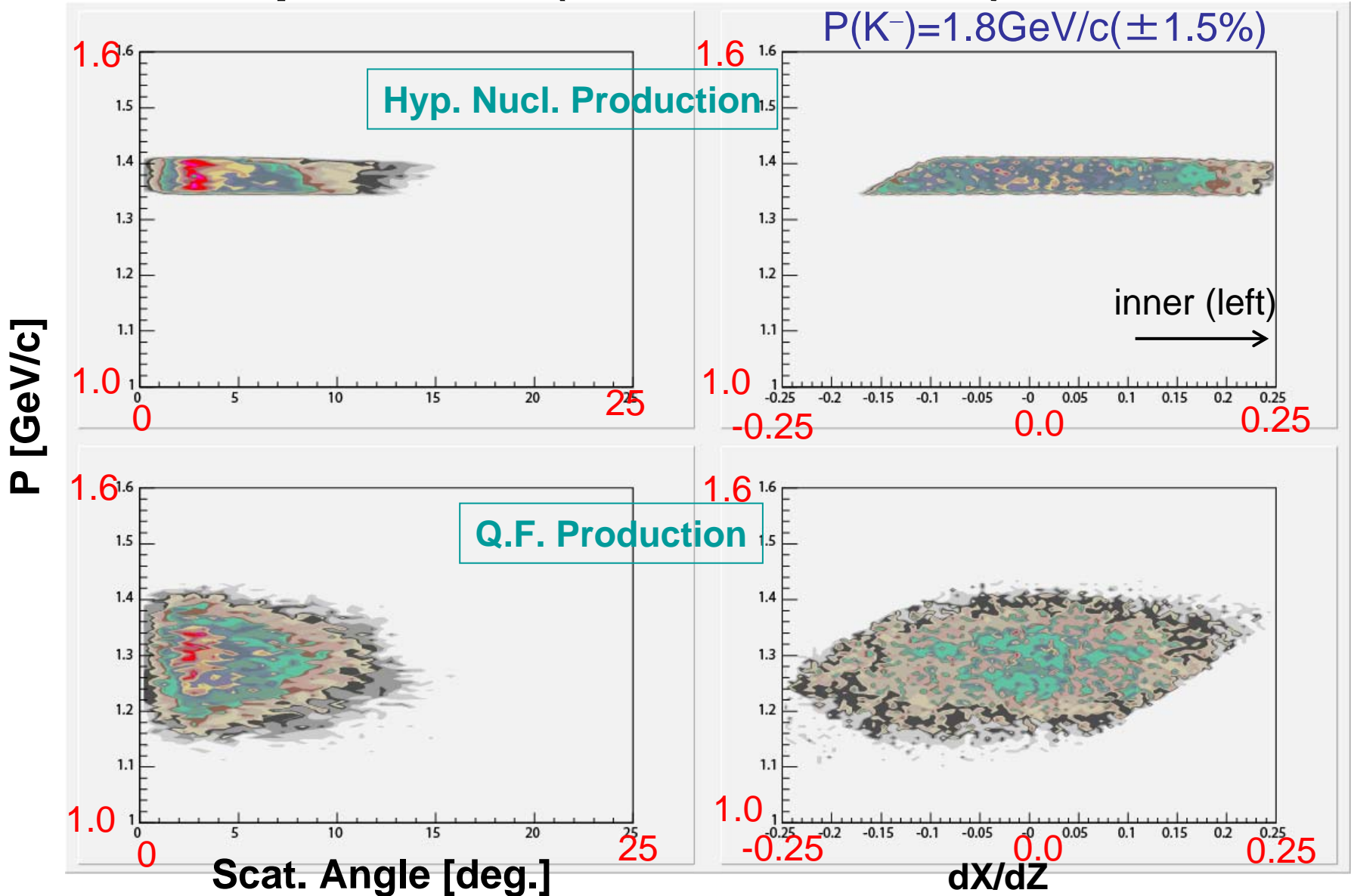
$p = 1.8 \text{ GeV}/c$



$p = 1.65 \text{ GeV}/c$

No decay B.G. !!

# Acceptance(SksPlus02) More...



# Characteristics of ( $K^-$ , $K^+$ ) reaction

- To convert proton to  $\Xi^-$
- $\Delta I=1$  reaction
  - If target of  $I=0$  is used,  **$I=1$  states** can be produced.
- Large momentum transfer  $q \sim 0.5 \text{ GeV}/c$ 
  - spin stretch states
  - smaller S-factor than ( $\pi^+$ ,  $K^+$ ) case of  $q \sim 0.4 \text{ GeV}/c$ .

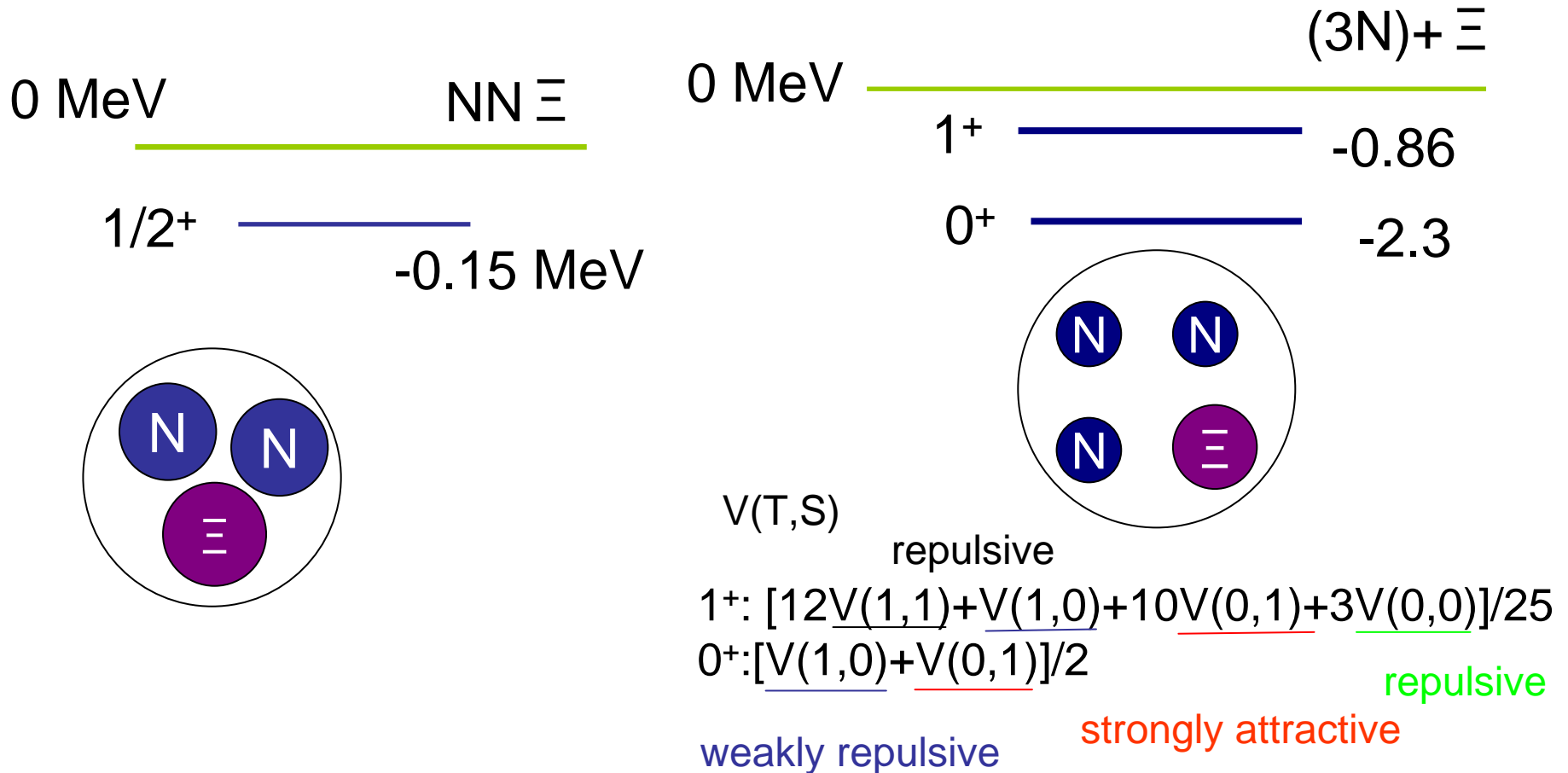
# $\Xi N$ interaction

- Exp. Information
  - $V_{\Xi} = \sim -14\text{MeV}$  from  $^{12}\text{C}(K^-, K^+)$   
note that for  $T=1$  state(s)
- ESC04 reproduces  $V_{\Xi} = -14\text{MeV}$ 
  - Strong Isospin dependence
    - $T=0$  is more attractive than  $T=1$
- NSC97e and f do not.
  - repulsive

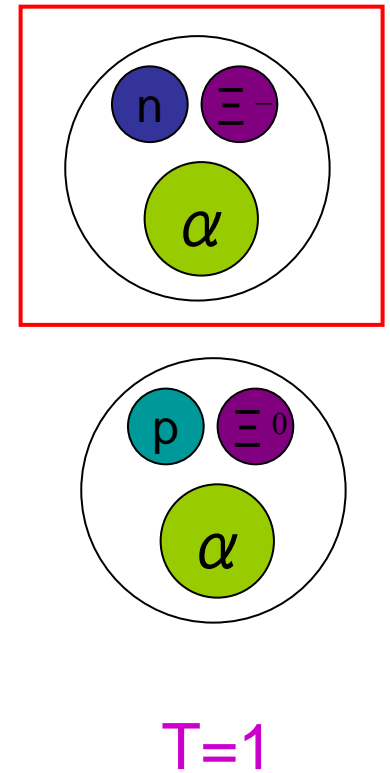
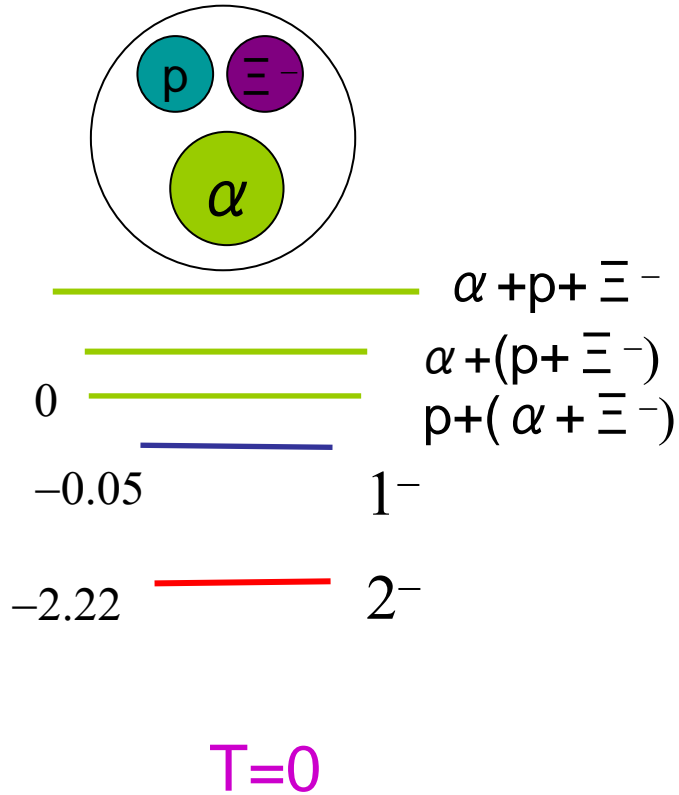
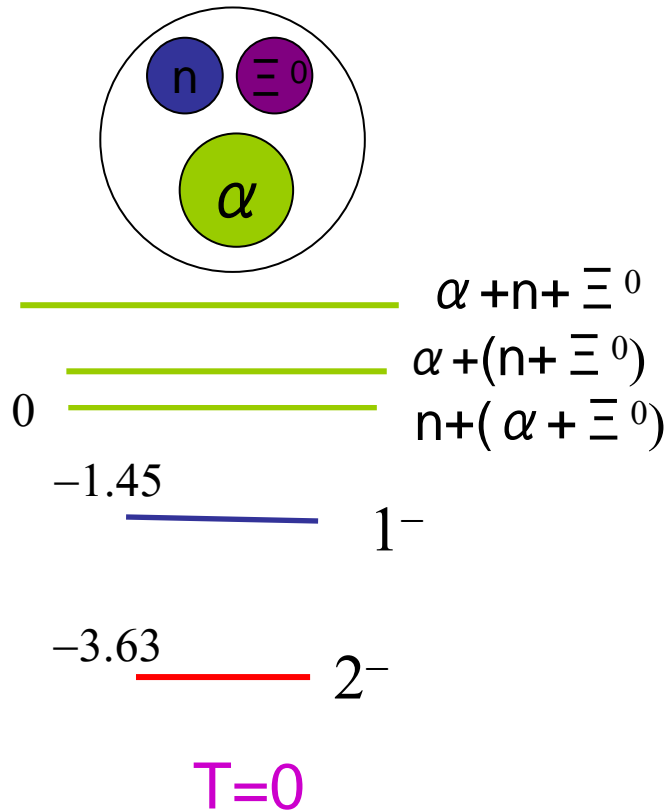


# Hiyama's calculation

ESC04



# Hiyama's calculation



# Hall Rayout (K1.8)

